Reg. No.:					
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## Question Paper Code: 70860

B.E./B.Tech. DEGREE EXAMINATIONS, NOVEMBER/DECEMBER 2023.

Fourth/Fifth/Sixth Semester

Civil Engineering

## MA 8491 - NUMERICAL METHODS

(Common to Aeronautical Engineering/Aerospace Engineering/
Agriculture Engineering/Civil Engineering/Electrical and Electronics Engineering/
Electronics and Instrumentation Engineering/Instrumentation and Control
Engineering/Manufacturing Engineering/Mechanical Engineering
(Sandwich)/Mechanical and Automation Engineering/Biotechnology and Biochemical
Engineering/Chemical Engineering/Chemical and Electrochemical
Engineering/Plastic Technology/Polymer Technology/Textile technology)

(Regulations 2017)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

PART A — 
$$(10 \times 2 = 20 \text{ marks})$$

- 1. What is the sufficient condition for the convergence of Gauss Seidel method?
- 2. What is the geometrical meaning of Newton's method?
- 3. What is interpolation?
- 4. Find  $\Delta(xe^x)$ .
- 5. Evaluate  $\int_{-1}^{1} (3x^2 + 5x^4) dx$  by Gaussian three point formula.
- 6. Why trapezoidal rule is called so?
- 7. Given y' = -y, y(0) = 1 find the value of y at x = 0.01 using Euler method.

- 8. Compare Taylor Series and Runge-Kutta method of fourth order.
- 9. Write the finite difference scheme of the differential equation y'' + 2y = 0.
- 10. Write down the Laplace and Poisson equation.

## PART B — $(5 \times 16 = 80 \text{ marks})$

- 11. (a) (i) Find a real positive root of  $3x \cos x 1 = 0$  by Newton's method correct to six decimal places. (8)
  - (ii) Apply Gauss-elimination method to obtain the solution of the system (8)

3x + 4y + 5z = 18, 2x - y + 8z = 13 and 5x - 2y + 7z = 20

Or

- (b) (i) Solve the following system of equations 10x 5y 2z = 3, 4x 10y + 3z = -3, x + 6y + 10z = -3 by Gauss-Seidel method. (8)
  - (ii) Find the largest eigen value of  $\begin{pmatrix} 5 & 0 & 1 \\ 0 & -2 & 0 \\ 1 & 0 & 5 \end{pmatrix}$  by power method. (8)
- 12. (a) (i) Prove that the following:
  - (1)  $E\nabla = \Delta = \nabla E$

(2)  $hD = \log(1 + \Delta) = -\log(1 - \nabla)$ . (8)

(ii) Find the values of y at x = 21 and x = 28 from the following data. (8)

X 20 23 26 29 Y 0.3420 0.3907 0.4384 0.4848

Or

- (b) (i) Form the divided difference table for the data given below. (8)  $X: -2 \quad 0 \quad 3 \quad 5 \quad 7 \quad 8$   $Y: -792 \quad 108 \quad -72 \quad 48 \quad -144 \quad -252$ 
  - (ii) Using Lagrange's formula, fit a polynomial for the given data below and hence find y(x=1). (8)

 $X: -1 \quad 0 \quad 2 \quad 3$ 

 $Y: -8 \ 3 \ 1 \ 12$ 

Y (Population in 1000) 40.62 60.80 79.95 103.56 132.65

(ii) Evaluate 
$$\int_{0}^{6} \frac{dx}{1+x^2}$$
 by Gaussian two point formula. (8)

Or

- (b) Evaluate  $\int_{1}^{1.4} \int_{2}^{2.4} \frac{dx \, dy}{xy}$  using Trapezoidal and Simpson's rules. Verify the result by actual integration. (16)
- 14. (a) (i) Use Taylor series method to find y at x = 0.1 and x = 0.2, given  $\frac{dy}{dx} = x^2 y, \ y(0) = 1. \tag{8}$ 
  - (ii) Apply Milne's method, find y(2) if y(x) is a solution of  $\frac{dy}{dx} = \frac{1}{2}(x+y), \ y(0) = 2, \ y(0.5) = 2.636, \ y(1) = 3.595, \ y(1.5) = 4.968.$ (8)

Or

- (b) (i) Using Runge-Kutta method, find y(0.1) given that  $\frac{dy}{dx} = x + y$ , y(0) = 1, h = 0.1. (8)
  - (ii) Using Adam's method, find y(0.4), given that  $\frac{dy}{dx} = \frac{xy}{2}$ , y(0) = 1, y(0.1) = 1.01, y(0.2) = 1.022, y(0.3) = 1.023. (8)
- 15. (a) Solve the Laplace equation  $u_{xx} + u_{yy} = 0$  over the square mesh of side four units satisfying the following boundary conditions:
  - (i) u(0, y) = 0,  $0 \le y \le 4$
  - (ii)  $u(4, y) = 12 + y, 0 \le y \le 4$
  - (iii)  $u(x, 0) = 3x, 0 \le x \le 4$
  - (iv)  $u(x,4) = x^2, \ 0 \le x \le 4.$  (16)

Or

- (b) (i) Solve  $u_{xx} = 2u_t$ , given u(0,t) = 0 = u(4,t), u(x,0) = x(4-x). Assume h = 1 find the values of u up to t = 5 by Bender-Schmidt's method. (8)
  - (ii) Solve numerically  $4u_{xx} = u_{tt}$  with the boundary conditions u(0,t) = 0, u(4,t) = 0 and the initial conditions  $u_t(x,0) = 0$ , u(x,0) = x(4-x) taking h=1 for 4 time steps. (8)